# A New Security Level Oriented Multisignature Scheme

**Abulameer Khalaf Hussain, Muthnna Abdulwahid Khudhair**

***Abstract*: This paper presents a new multisignature scheme. The idea behind this scheme is that all authenticated users in the system are classified according to their security levels . Each level has its own trusted group manager. To generate the signature, the proposed system selects one of these levels .Each level consists of a group of users . Each user has its own private and public keys. In addition, this scheme implements the cascade encryption for the generated signature, and thus it is necessary to perform the cascade encryption to use a global private key for each level. The system also assigns trustworthiness score for each user to select the proper one to sign on the behalf of his/her group in that level. Finally, the generated multisignure is proved to be more secure and thus it can be used in sensitive applications.***

***Index Terms*: Digital Signature, multisignature system, Security Levels, Multi-level proxy signature.***

## I. INTRODUCTION

A multisignature scheme is defined as a digital signature scheme that gives the permission to multiple signers to generate a single signature in a collaborative and simultaneous manner [1,2]. In some applications, there are different roles/ positions associated for co-signers in a signing group and therefore have different management authorization capabilities. Thus, multisignatures generated by the same group of co-signers with different signing orders often imply different meanings. Some workflow management systems have addressed this concern in literature [3,4], in which a multisignature has to be checked against the organizational structure of the signing group.

Different previous studies of structured multisignature schemes such as Mitomi and Miyaji had proposed two schemes that respectively based on discrete logarithm problem and integer factorization [5]. Also in [6], Kotzanikolaou et al. specified an attack against the Mitomi-Miyaji's discrete logarithm based scheme and they proposed a modification for it. However, their modification is not secure as addressed in [7]. Recently, Boneh, Shacham and Lynn proposed a new signature scheme based on the Gap Diffie-Hellman (GDH) problem [8].

Multisignature scheme gives the ability for different signers signing the same document. A verifier person or any entity is convinced that each signer participated in signing by transmitting a multi-signature instead of individual signatures. So multi-signature schemes can greatly save on communication costs. Multisignatures were first introduced by Itakura and Nakamura [9] and have been the topic of muchresearch [10-12]. Micali, Ohta and Reyzin [5] also gave the first strong concept of security of multisignatures. A vaiant of Micali-Ohta-Reyzin model was given by Boldyreva [12] . Multisignatures is related to the aggregate signature. Boneh,Gentry,Lynn and Shacham [13] defined an aggregate signature scheme. Unlike multi-signature, aggregate signature aggregate signature scheme provides a method to aggregate signature by signature on different messages. Alexandra Boldyreva et al. [14] propose a new primitive that they call ordered multi-signatures (OMS) and a formal security model for ordered multi-signatures.

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## II. RELATED WORKS

Lihua,Wang et al. proposed an ID-based series-parallel multisignature scheme based on pairings . In this scheme, signers in the same subgroup sign the same message, but those in different subgroups sign different messages. This scheme is proven secure against forgery signature attack from parallel insiders under the BDH assumption [15].

A research had been proposed in [16] to propose a new multi-level proxy signature scheme based on q-SDH assumption combining with Wei and Yuen's short signature. The properties of this scheme are non-repudiation, unforgeability, undeniability . Therefore, the proxy signature right can come true step by step under agreement.

In [17] the authors presented a new multisignature scheme which can be used in client-server model of group communication systems to deal with certain problems that arise while implementing safe delivery rule in such systems. The proposed multisignature scheme enables the group communication server to combine all acknowledgements of a certain message from all group members into a single group-acknowledgement message which has a constant size and send it to the sender of the message.

A research was proposed to resist clerk and rogue-key attacks. In the proposed scheme, multiple signers can generate a multisignature for the message with the signers' secret keys, and the specified group of verifiers can cooperate to verify the validity of the multisignature with the signers' public keys and the verifiers' secret key [18].

In [19 ] , the authors proposed a new efficient identity-based key-insulted multisignature scheme . The aim of this paper is for facilitating group-oriented applications and mitigating the impact of key exposure. Each user ,in this scheme, has the ability to periodically update his private key but the public key remains unchanged. This scheme has the properties of unbounded time periods and random-access key-updates. The scheme is compared with previous works and it is formally proven its security of unforgeability against existential forgery under adaptive chosen-message attacks (EF-CMA) in the random oracle model.

A paper proposed in [20] two structured multisignature algorithms, one based on the RSA scheme and the other on an ElGamal-type scheme. Incorporation of both order-free and order-sensitive multisignature algorithms together is shown to construct a generalized multisignature algorithm.



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Another research proposed a multi-signature scheme, in which each signer can express her intention associating with the message to be signed. Signers' intentions mean a kind of information which can be newly attached signature in signers' generating to it. First, the authors considered a multi-signature scheme that realizes the concept of signers' intentions by utilizing existing schemes, and then name it as a primitive method. After that, they introduced the proposed multi-signature scheme which is more efficient than the primitive method in terms of the computational cost for verification and in view of the signature size [21].

In [22] the authors gave the model of ID-based designated verifier proxy multi-signature and presented a new ID-based designated verifier proxy multisignature scheme. The security of this scheme is based on the computational Diffie-Hellman (CDH) problem and it is highly efficient.

## III. PROPOSED SYSTEM

The scheme in this paper generates a multisignature of an authenticated group of users. The users are first classified according to their security level in the system. For this purpose, the scheme classifies security levels depending on two types of parameters. The first parameter is the data types, these types are arranged as: classified, secret, and top secret. The second parameter is the degree of trustworthiness of each user within each level (TW).

If we suppose that the level set is DL={C,S,T} , where C denotes classified level , S denotes secret level ,and T denotes top secret level. Suppose also the set of authenticated users of C level is UC={uc1,uc2,….,ucn1} , the set of authenticated users of S level is SU={su1,su2,…,sun2} , and the set of authenticated users of T level is TW={tw1,tw2,….,twn3}.

The multisignature of this group is generated using the RSA scheme. Accordingly, each authenticated user must have a set of private keys, d. These private keys are calculated by choosing two prime numbers ,p and q, for each level and it needs a set of corresponding public keys , e.

Table 1 illustrates these sets of both security levels and authenticated users in each level.

**Table1: Security Level Classifications.**

| Level Number | Level Type | Authenticated Users | public keys(e) | private keys(d) | Trustworthiness Scores |
|---|---|---|---|---|---|
| 1 | Classified( C) | UL11<br>UL12<br><br>UL1n | eL11<br>eL12<br><br>eL1n | dL11<br>dL12<br><br>dL1n | twL11<br>twL12<br><br>twL1n |
| 2 | Secret (S) | UL21<br>UL22<br><br>UL2m | eL21<br>eL22<br><br>eL2m | dL21<br>dL22<br><br>dL2m | twL21<br>twL22<br><br>twL2m |
| 3 | Top Secret (T) | UL31<br>UL32<br><br>UL3k | eL31<br>eL32<br><br>eL3k | dL31<br>dL32<br><br>dL3k | twL31<br>twL32<br><br>twL33 |

For each level, there is a global private key (dg) and a corresponding public key (eg).

These keys are used to cascade the encryption process to enhance the security of the signature. Now assume we want to encrypt a message M with a certain private key of a user in one of the levels.

The algorithm below illustrates the steps of generating a secure multisignature :

Algorithm

Sender Side

1: Let Mi be the message for each level , i , Ci the ciphertext of each level.

2: Let Li be the indicated level

3: Select two prime numbers for each level (Li) . Let these prime numbers are pLi and qLi.

4: n(Li)=PLi* qLi

5: ϴLi=(pLi-1)(qLi-1)

6: Choose eLi

7: Calculate the corresponding private key from the following formula:

dLi=inv(eLi)mod ϴLi

8: Generate the group signature for each element in the chosen level as follows :

A: Ci=Mdi mod n

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B: The group signature is :

CLi=Md1||Md2||…….Mdn

= C1||C2||……..Cn

C: Choose the proper trustworthiness score (TUSLi) to be a candidate signature on the behalf of the group to do the next step.

D: To enhance security we encrypt this signature with the global private key of that level.This is of the general form :

C1=E(M)

C2=E(E(M))=E(C1) then our group signature will take the following form:

Cdouble=( CLi )dgi

=( C1||C2||…….Cn )dgi

This represents the group signature for each level which is performed by the candidate user.

9: The above steps are repeated for each authenticated user in the chosen level.

10: The trusted manager chooses the proper trustworthiness score (TUSLi) to be a candidate signature on the behalf of the group .

Receiver side

Decrypt the ciphertext using the corresponding global public key ,egi :

Mdouble=( CLi )e gi

=( C1||C2||…….Cn )egi

=( C1||C2||…….Cn )

=Me1||Me2||….Men)

Moriginal = M||M||… M

If all M are the same so the signature is authenticated.

## IV. RESULTS

Suppose we choose level 1 , L1 . Let pL1=7 and qL1=11.

So nL1= 7*11=77 , ϴL1=(pL1-1)((qL1-1)= (7-1)(11-1)=60

We choose 3 users from level 1 , namely UL11,UL12,and UL13

Select public keys for these users as , eL11=13,eL12=7,and eL13=11.

The scores assigned to these users are: UL11=60, UL12=30, UL13=50.



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Let the message M=18 , calculate the corresponding private keys as following:
dL1=inv(13)mod 60=37
dL2=inv(7) mod 60=43
dL3=inv(11) mod 60= 11
The generation of each ciphertext is explained below:
$CL11=18^{37}$ mod 77= 39
$CL12=18^{13}$ mod 77=46
$CL13=18^{11}$ mod 77=51
The user selected to sign on behalf of this level is UL11 who represents the candidate user , because of his/her high score.
So first we concatenate the above three ciphertext which represent the signature of each user in this level as explained below:
Sig= 3946
Then UL11 again signs this signature with his/her private key,37.
$SigK=(3946)^{37}$ mod 77=68
Then he/she signs this result with the global private key using a global public key which is calculated as follows:
Let the global public key=9
So the global private key= inv(9) mod 60 =7,and the final digital(FSG) signature is :
FSG=(68)7 mod 77 = 40

## V. ANALYSIS AND CONCLUSION

This proposed system generates a new scheme secure multisignature. The secrecy of this system is more powerful than other multisignature schemes. It implements the a security level classification and one of them is selected to generate the digital signature so it is considered a general method of security level classification. Each authenticated user had been assigned a trustworthness score depending on his/her experience in dealing with different classes of secret information. The system also uses the cascade encryption to provide more secrecy of the generated signature and thus it assists in increasing secrecy of the message. The system also assume of the message in a strict manner. In addition the proposed system provides properties of a strong muktisignatuthare that enables the system to resist against different attacks such as colluding attack and denial of service . One of these properties is that unforgeablility because only authenticated users of the group can create valid group signatures .The second property is that anonymity since for a given message and its signature, the identity of the individual signer cannot be determined without the group manager's global private key. The applications of this proposed system are: bank funds transfer, military sensitive applications, and marketing.

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